

The Development and operational implementation of GRAPES Global ensemble prediction system at CMA

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Outline

- SV-based initial perturbations
- Representations of model uncertainties
- The performances of GRAPES-GEPS
- Summary and future work

The GRAPES Global Singular Vectors

- **G**lobal/**R**egional **A**ssimilation **P**rediction **S**ystem (**GRAPES**) at CMA
- **GRAPES** global SVs with the Euclidean vector $\hat{X}_i(t_0)$ are calculated as follows:

$$\left(\mathbf{E}^{-\frac{1}{2}} \mathbf{L}^T \mathbf{P}^T \mathbf{E} \mathbf{P} \mathbf{L} \mathbf{E}^{-\frac{1}{2}} \right) \hat{X}_i(t_0) = \lambda_i^2 \hat{X}_i(t_0)$$

$$X_i(t_0) = \mathbf{E}^{-\frac{1}{2}} \hat{X}_i(t_0)$$

$$X = (u', v', (\theta')', (\Pi')')^T$$

- **L** : Tangent linear model (TLM)
 - **L^T** : Adjoint model (ADM)
 - **P** : Projection operator
 - **E** : Total energy norm
- Total energy norm **E** is based on variables of GRAPES TLM

$$\iiint_V \left(\frac{\rho_r \cos \varphi}{2} (u')^2 + \frac{\rho_r \cos \varphi}{2} (v')^2 + \frac{\rho_r \cos \varphi C_p T_r}{(\theta_r)^2} ((\theta')')^2 + \frac{\rho_r \cos \varphi C_p T_r}{(\Pi_r)^2} ((\Pi')')^2 \right) dV$$

u' : the perturbations of u

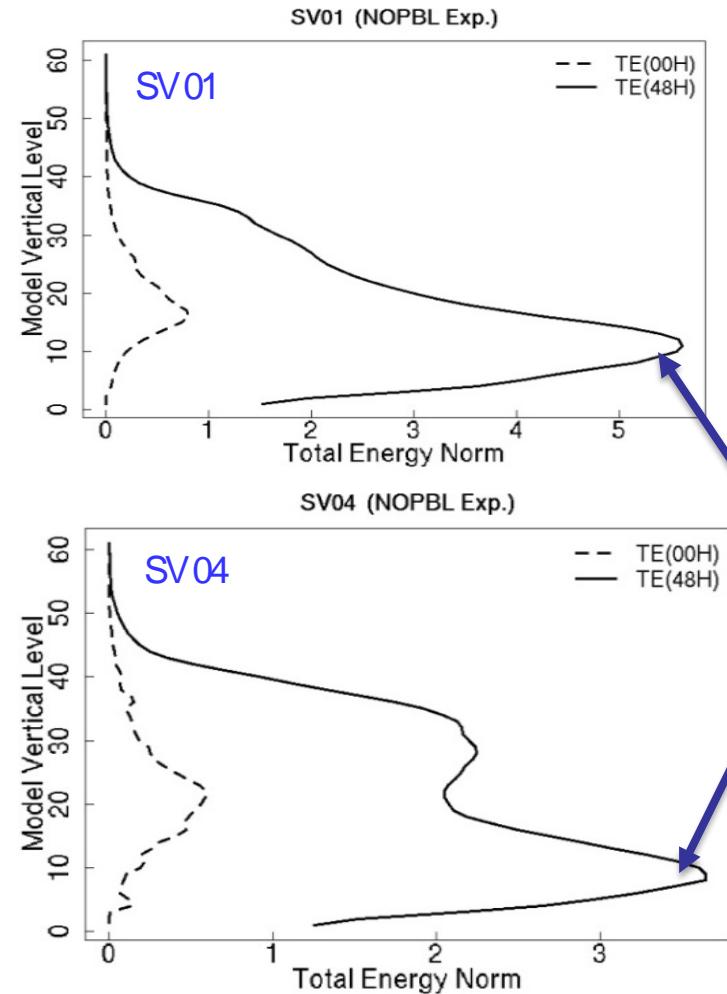
v' : the perturbations of v

$((\theta')')$: the perturbations of perturbed potential temperature θ'

$((\Pi')')$: perturbations of perturbed Exner pressure Π'

GRAPES Singular Vectors (Version 1)

- 48h optimization time interval(OTI)
- 2.5 degree horizontal resolution and 36 vertical levels
- **Localized regions:** Northern Hemisphere extra-tropics (30°–80°N); Southern Hemisphere extra-tropics (30°–80°S)
- **TLM and ADM (version 1):** dynamical core of GRAPES_GFS without **Linearized physics schemes**
- **The trajectory of TLM is from forecast of dynamical core of GRAPES_GFS**
- Iteration times of Lanczos Algorithm is 50, and 30 SVs are obtained approximately



the shallow unreasonable fast-growing structures in the lower level of model near surface was observed in evolved SVs.

Typical total-energy SVs

- The typical structures of SV based on total-energy norm

Buizza and Palmer(1994); Lawrence et al (2009); Leutbecher (2012)

- At initial time:

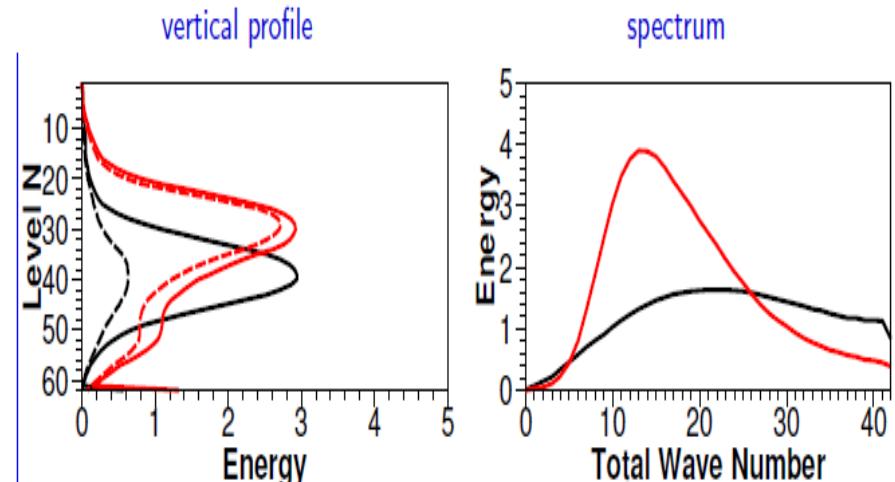
- the energy maximum of SVs is located in the middle troposphere, and potential energy is dominant
- westward tilt with height at initial time

- At final time

- the upward energy transfer to higher troposphere and downward energy transfer toward lower troposphere, the kinetic energy of SVs is dominant at final time
- upscale energy transfer with a pronounced final-time energy spectral

—: total energy; - - -: kinetic energy

Northern hemisphere extra-tropics, 2006032100



200 hPa ↔ level 20 300 hPa ↔ level 27
 500 hPa ↔ level 35 700 hPa ↔ level 42
 850 hPa ↔ level 48 925 hPa ↔ level 52

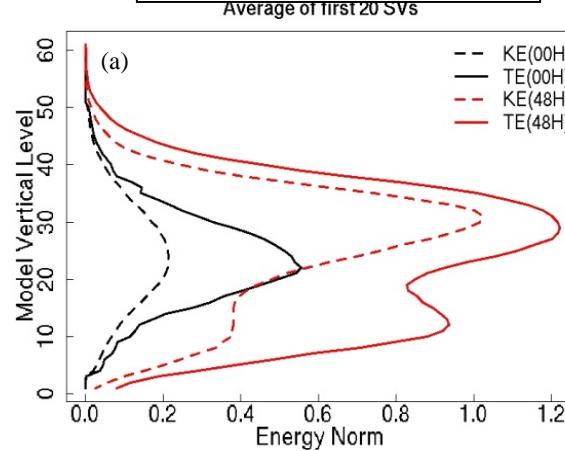
Leutbecher (2012)

wave number	wave length
5	8000 km
10	4000 km
20	2000 km
40	1000 km

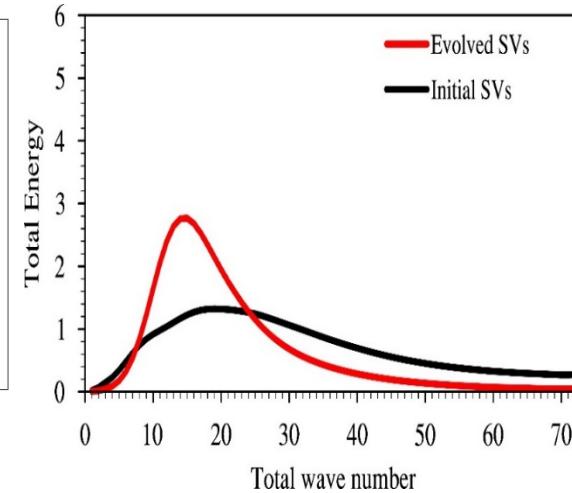
Improved GRAPES SVs (Version 2)

- **Localized regions:** Northern Hemisphere extra-tropics (30°–80°N); Southern Hemisphere extra-tropics (30°–80°S)
- **TLM and ADM (version 2)** with Linearized PBL scheme
- **The trajectory of TLM is from forecast of GRAPES_GFS**

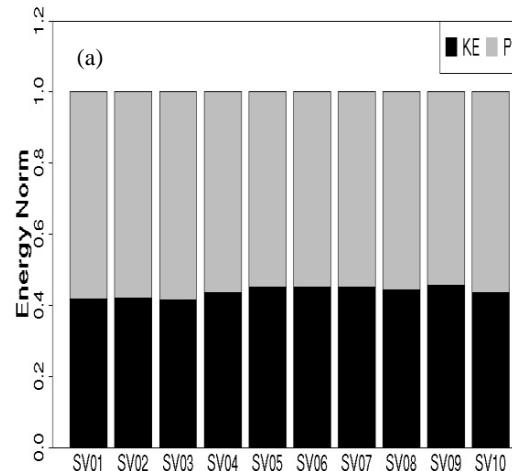
vertical profile



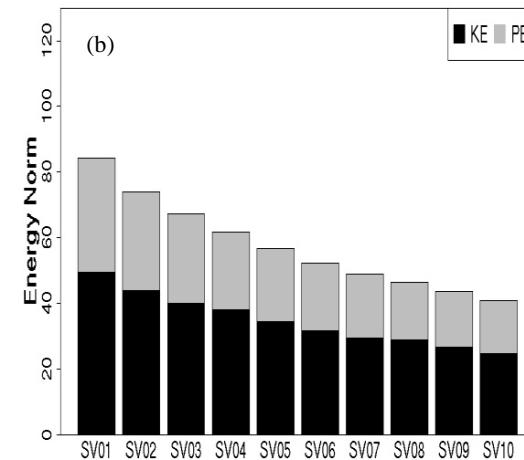
spectrum



Energy partition at Initial time



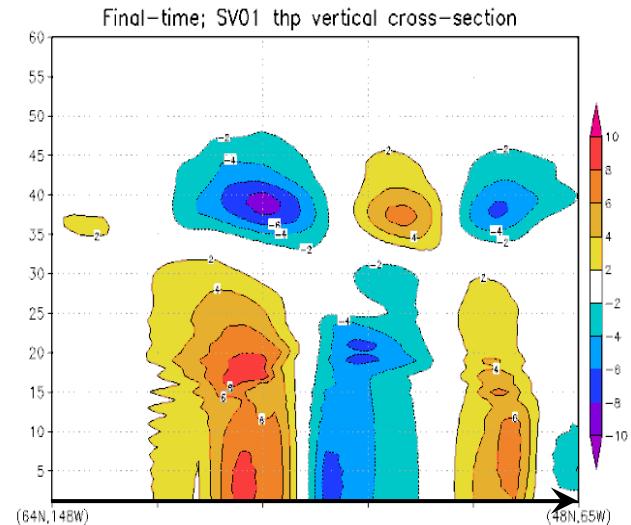
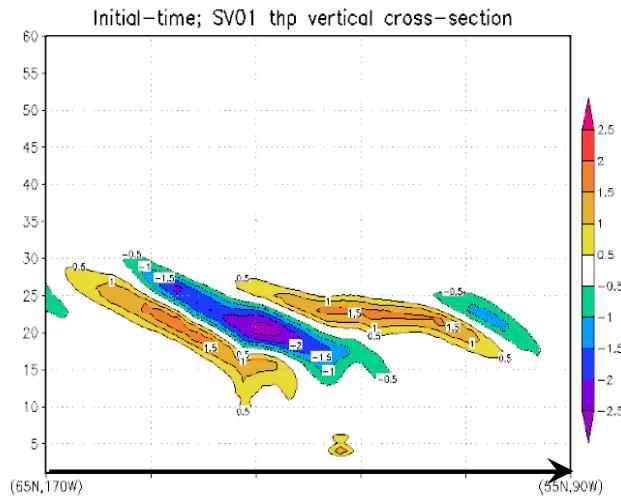
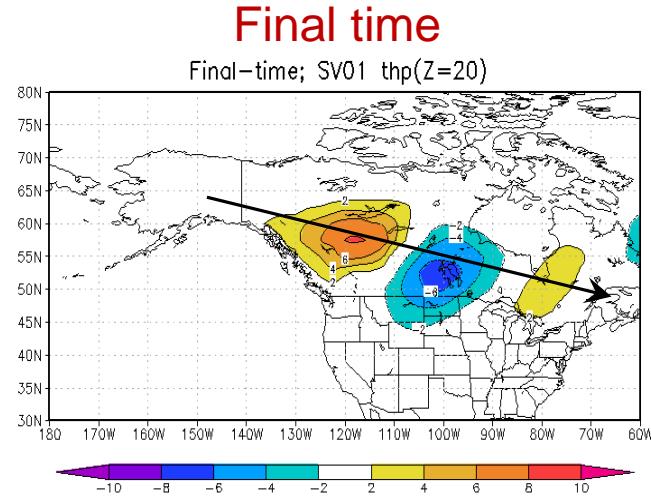
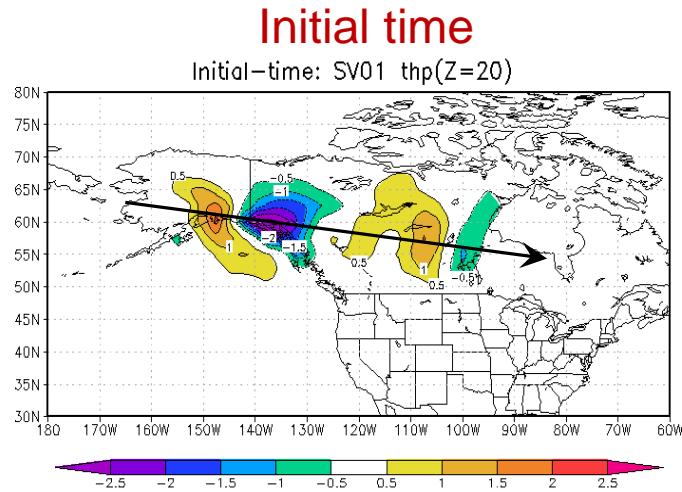
Energy partition at final time



- ✓ Typical *energy vertical profile* observed in GRAPES SVs at initial time and final time.
- ✓ The energy spectrum of GRAPES SVs shows *upscale energy transfer* at final time

The distribution of improved GRAPES NH SVs (1)

SV01- potential temperature perturbation (*1000), 8 May 2013,00UTC

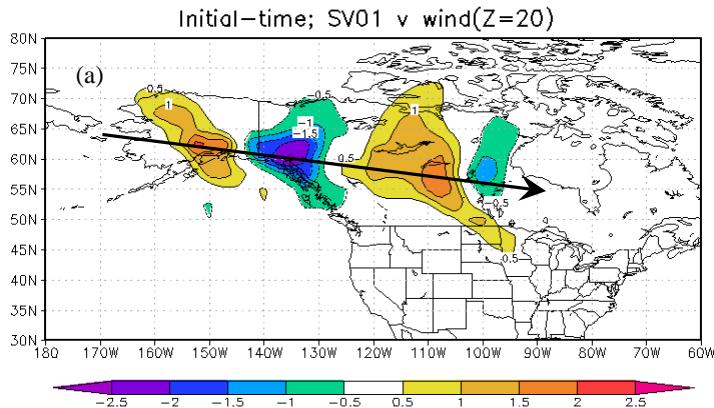


Typical *westward tilt* structure is observed in GRAPES SVs at initial time, and barotropic structure without obvious tilt is shown at final time

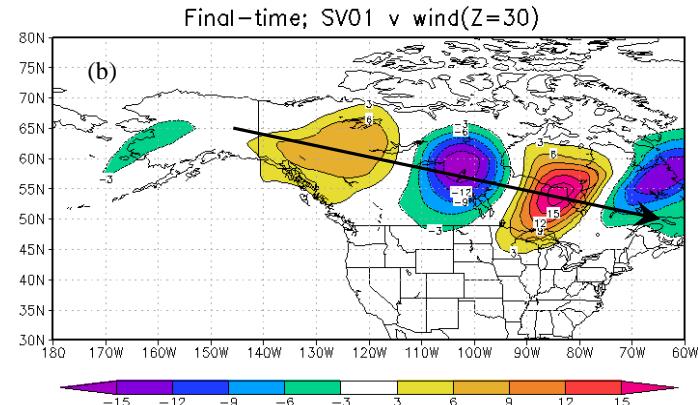
The distribution of improved GRAPES NH SVs (2)

SV01- u wind perturbation (*1000) , 8, May, 2013,00UTC

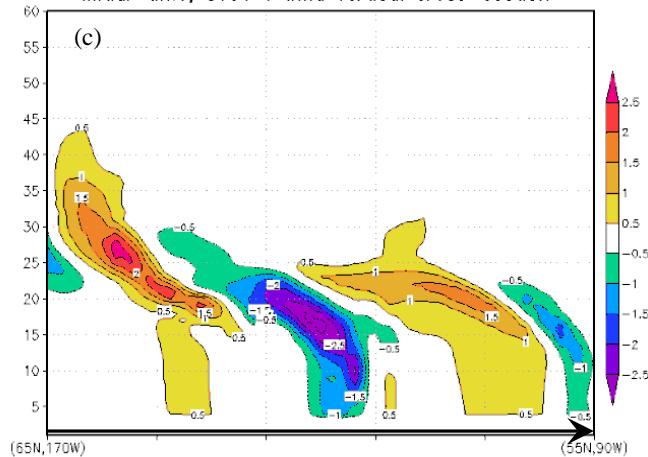
Initial time



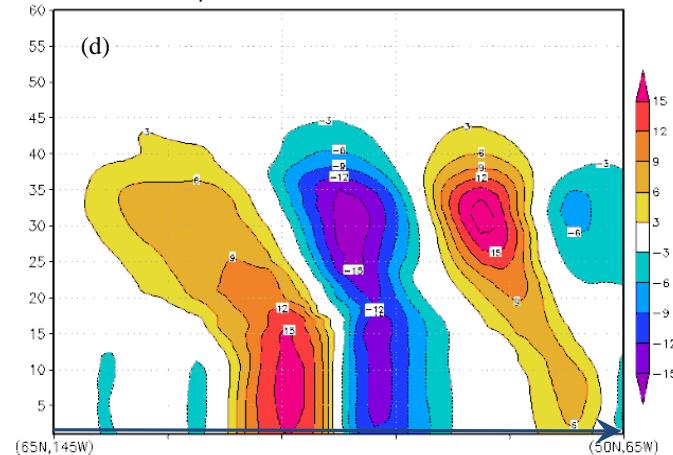
Final time



Initial-time; SV01 v wind vertical cross-section



Final-time; SV01 v wind vertical cross-section

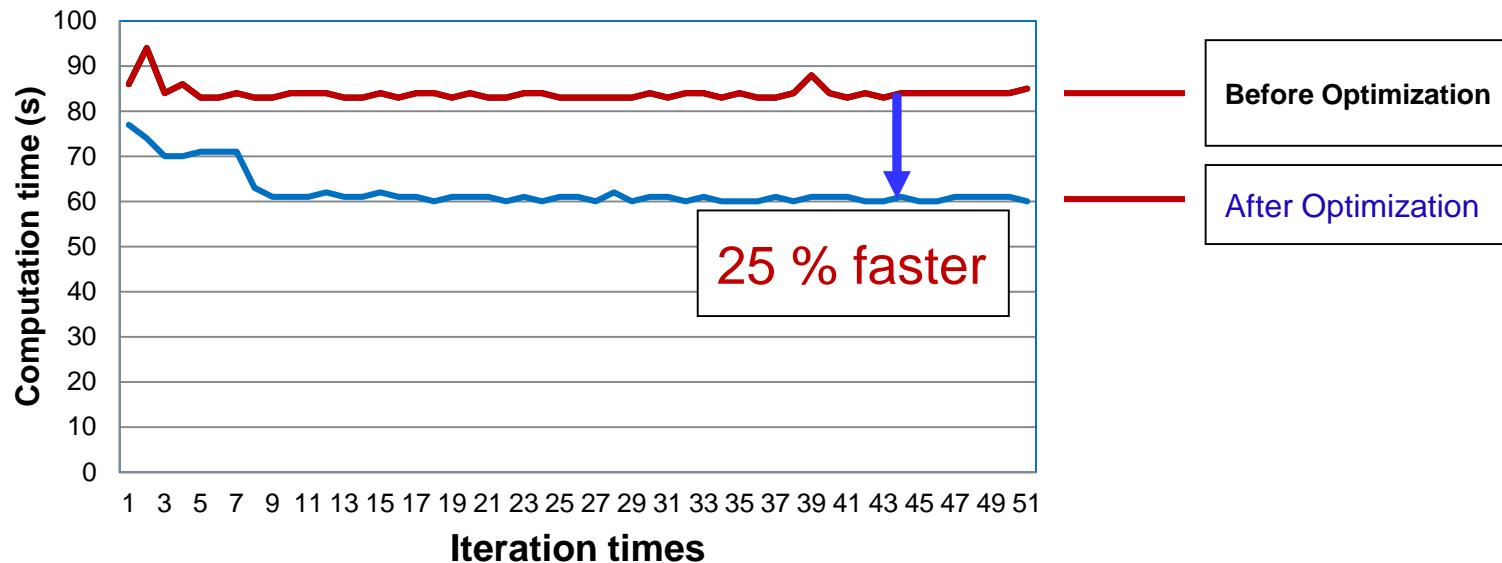


Besides the *westward tilt* structure SVs at initial time, and *Upward energy transfer* and *downward energy transfer* (kinetic energy) are observed at final time

Improving computational efficiency of GRAPES SVs

- The computation of ADM in SV calculation is most time consuming part
- The computation of the ADM are improved greatly by two aspects:
 - optimize the use of GCR in the ADM
 - increase the computation nodes
- The optimization reduces the computation time from **73** minutes to **55** min on IBM Flex P460

SVs calculation time for each iteration



- **37 minutes** on new HPC "PI-Sugon "at CMA (2018)

SV-based Initial Perturbations for GRAPES ensemble

The initial perturbations are obtained from the singular vectors via a multivariate Gaussian sampling technique (Leutbcher, 2008)

Main steps :

- (1) Calculating the rescale factors for the SVs based on standard deviation of analysis error: β_j

$$f_j^2 = \sum_{i=1}^N (u_i' / e_u)^2 + (v_i' / e_v)^2 + ((\theta_i')' / e_\theta)^2 + ((\Pi_i')' / e_\Pi)^2$$

$$\beta_j = \gamma / \bar{f}_j$$

The GRAPES SVs: $\hat{X}^{(j)} = (u', v', ((\theta')', ((\Pi')'))$

$e_u, e_v, e_\theta, e_\Pi$: estimated magnitude of standard deviations of analysis errors

γ : The empirical parameter to generate adequate ensemble spread

- (2) Using coefficients from random vector with Gaussian distribution to make linear combinations of rescaled SVs to get linearly sampled perturbations

$$P_i = \sum_{j=1}^N \alpha_{i,j} \beta_j \hat{X}^{(j)} \quad i = 1, 2, \dots, M$$

the coefficients $\alpha_{i,j}$ are random number with distribution of $N(0,1)$

SV-based initial perturbations for GRAPES-GEPS

(3) The SV-based initial perturbations with the component of evolved SVs

Evolved SVs provided an easy way to include more stable and large-scale directions in generation of EPS initial perturbation (*Barkmeijer et. al, 1998*)

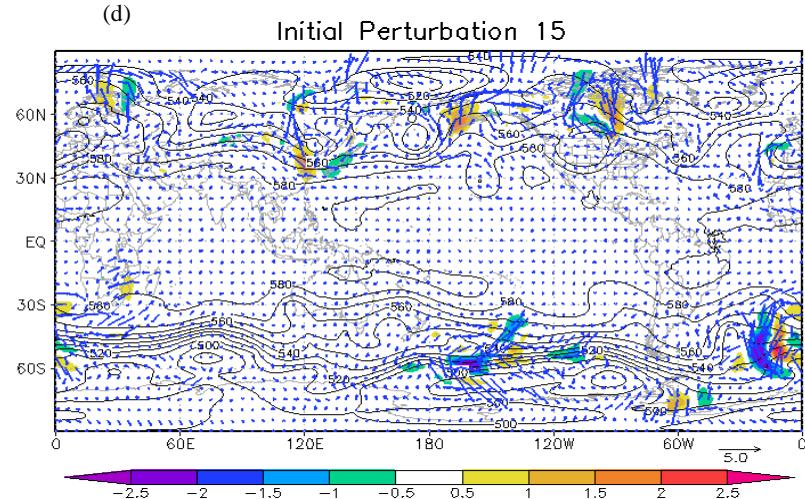
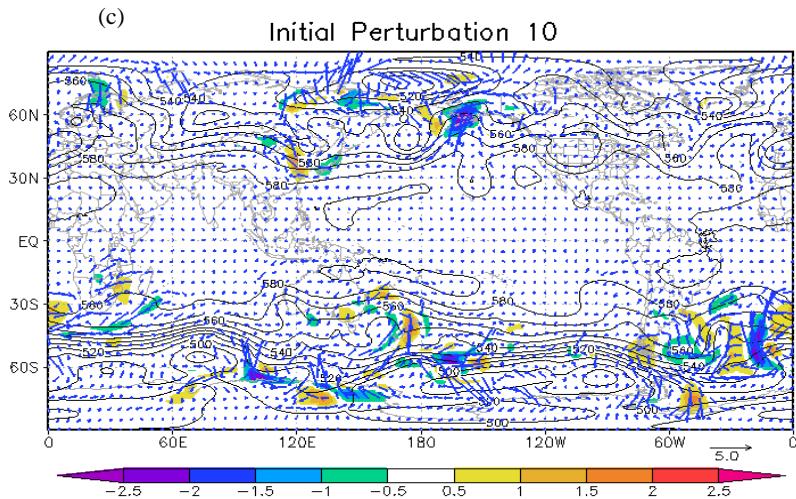
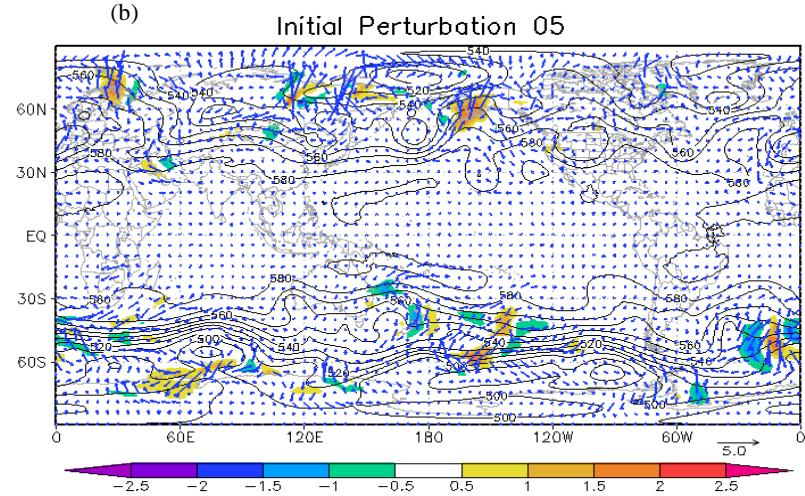
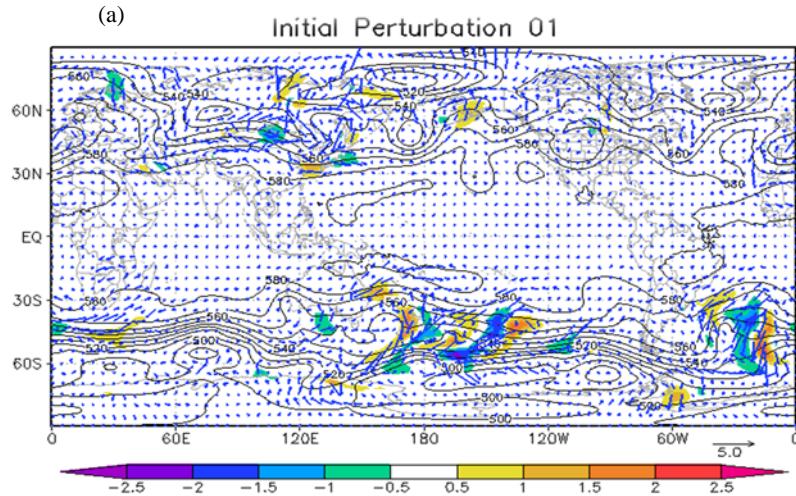
$$Pert_i = \underbrace{(1 - a)P_i(d, 0)}_{\text{INISV}} + a \underbrace{EP_i(d - 2, +2d)}_{\text{EVOSV}}$$

(4) Adding and subtracting linearly combined SVs from analysis (from GRAPES 3Dvar/4Dvar) to construct **perturbed initial conditions** for GRAPES global ensemble

$$X_i = X_A \pm Pert_i$$

The Structure of Initial Perturbations

500 hPa geopotential height, temperature perturbation (shaded); wind vector perturbation (arrows)



20 May, 2013, 00UTC

Ensemble Experiments based on Initial Perturbations

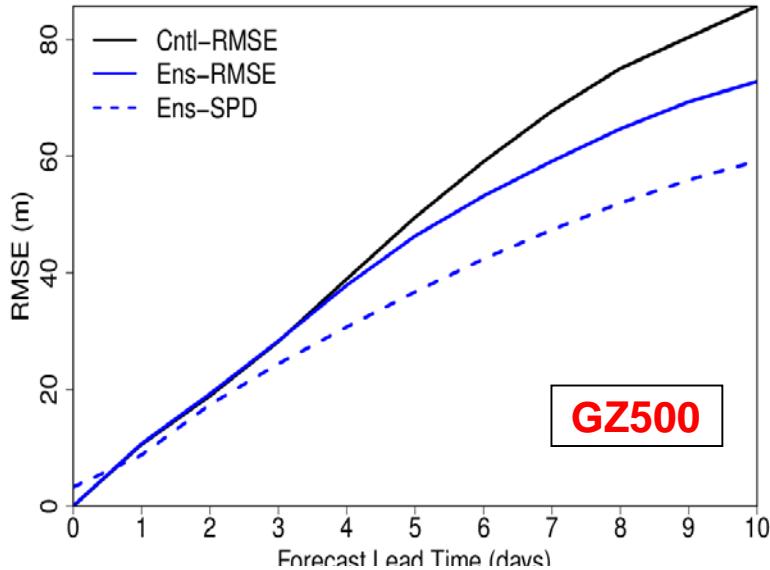
- **Exp. INISV**: Initial perturbations generated from initial SVs
- **Exp. EVOSV** : initial perturbations generated from initial SVs and evolved SVs ,coefficient α is 0.1)

Configuration of GRAPES-GEPS

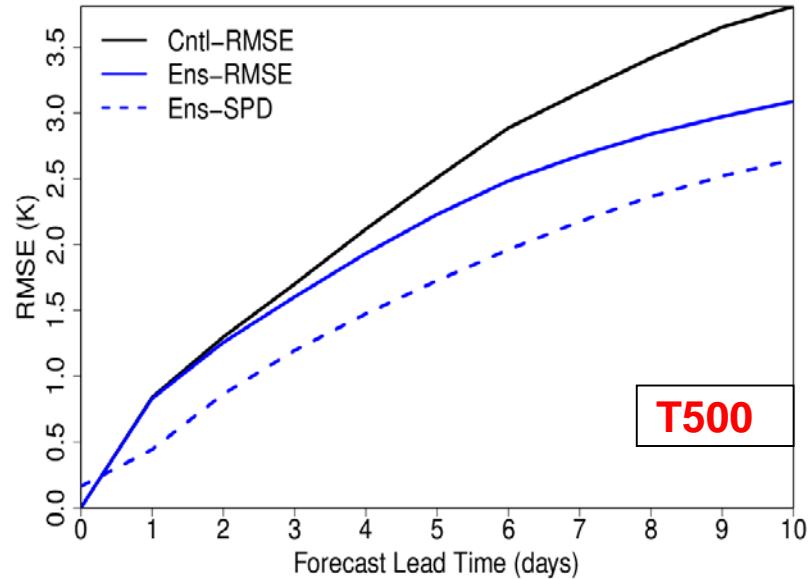
Experiment period	May 1- 31, 2013 ; 31days
TLM/ ADM model for SVs	Horizontal resolution: $2.5^\circ \times 2.5^\circ$; Vertical level: 60
Linear physics in TLM/ADM model	Linear PBL scheme
SVs computation area	NH : 30° N~ 80° N ; SH : 80° S~ 30° S
OTI of SVs computation	48h
Ensemble size	41 (40 perturbed member + control)
Forecast length of EPS	10 days
Initial analysis	GRAPES-3DVar ($0.5^\circ \times 0.5^\circ$; 60 levels)
resolution of GRAPES_GEPS	Horizontal resolution: $0.5^\circ \times 0.5^\circ$; Vertical level: 60

RMS ERROR AND ENSEMBLE SPREAD

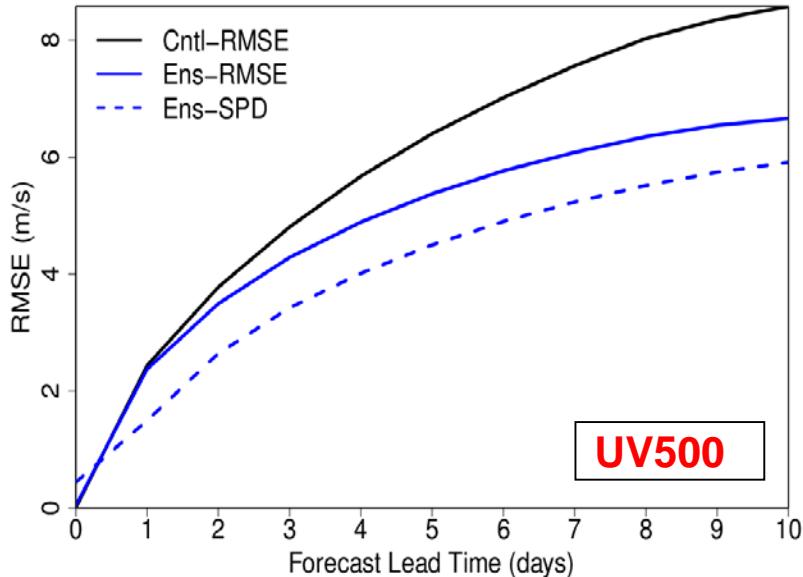
RMSE/SPD GZ500 over NH



RMSE/SPD T500 over NH

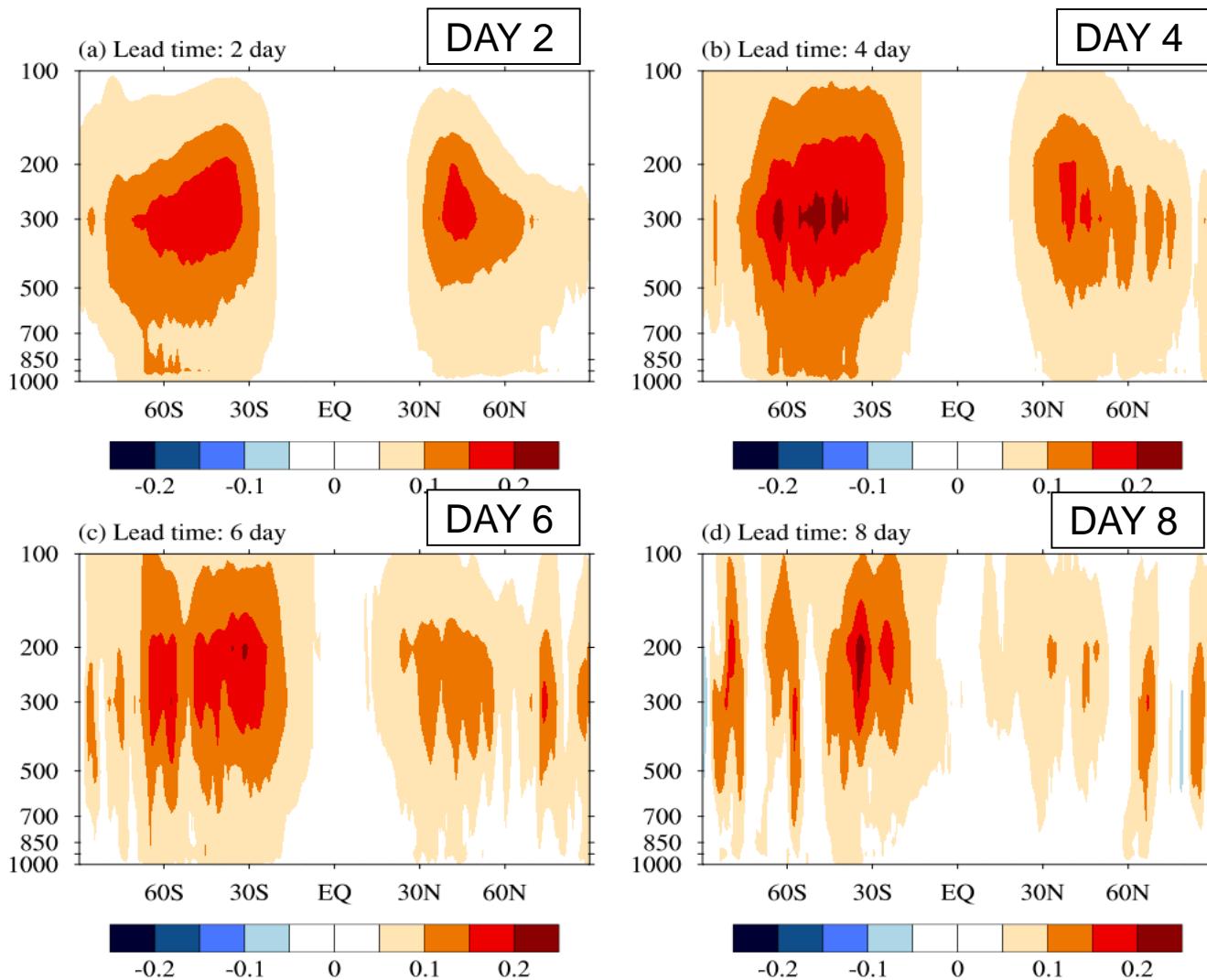


RMSE/SPD UV500 over NH



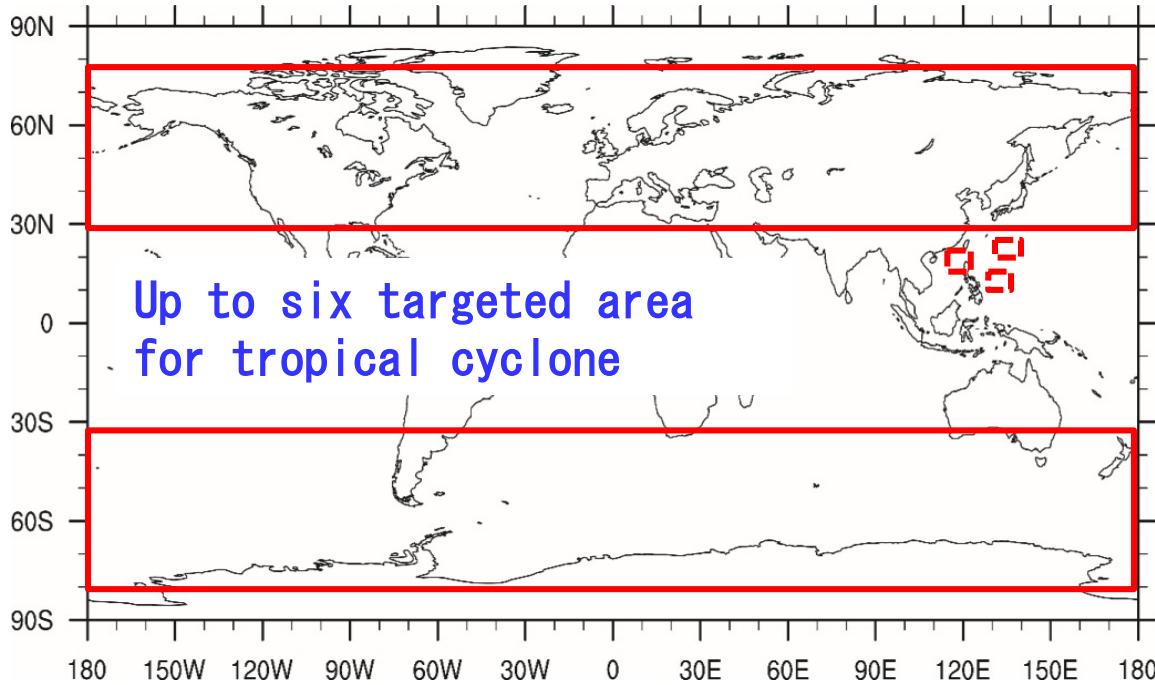
- RMSE of ensemble mean is smaller than that of Cntl, indicating the improvement of EPS
- The relationship between ensemble mean error and ensemble spread is reliable

Ensemble Spread difference (EVOSV-INISV)

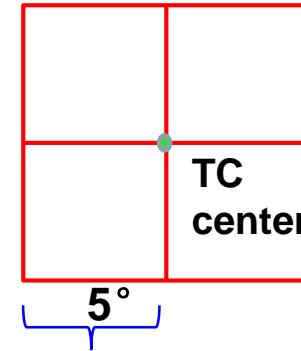


- Larger ensemble spread in EVOSV experiment at different lead times

SVs for tropical cyclones (TCSV) and initial perturbations



TCSVs targeted areas



- Lanczos iteration times : 20
- Linearized PBL, and **LSC** scheme

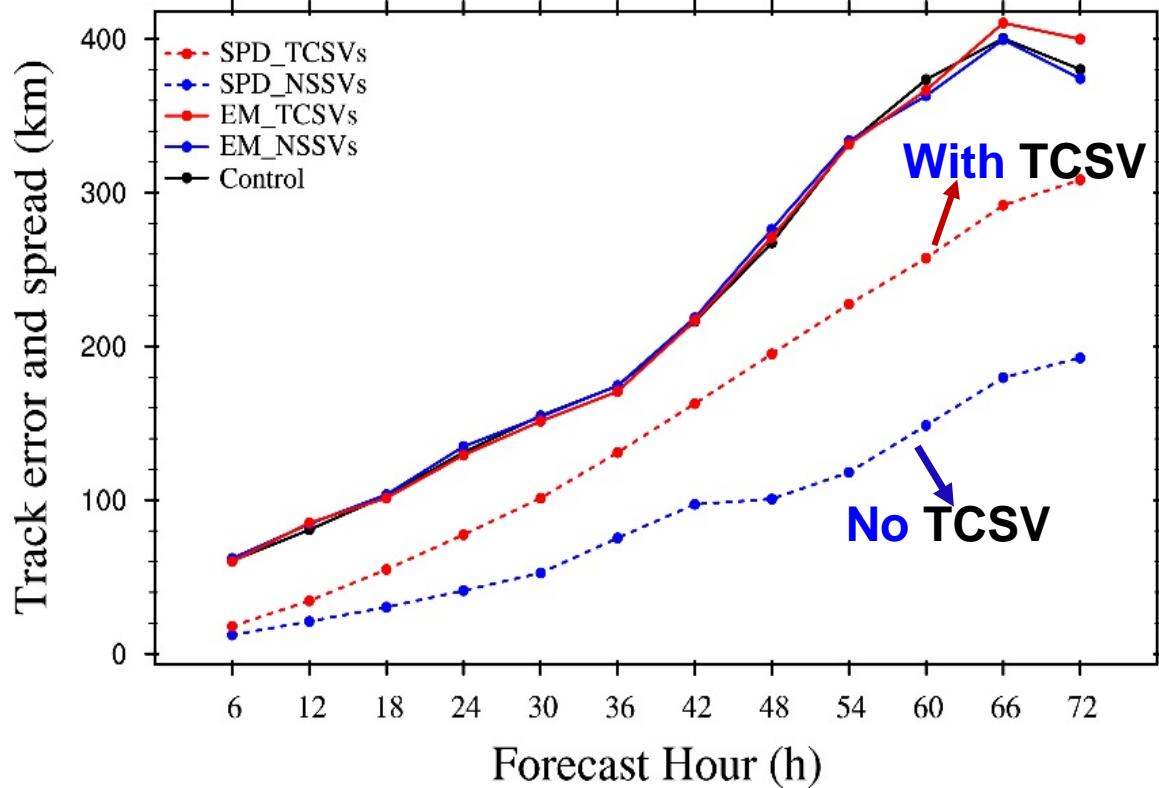
- **SVs-based Initial perturbation with TCSVs included**

$$\text{Pert}_i = \underbrace{(1 - a) P_i(d, 0)}_{\text{INISV}} + a \underbrace{EP_i(d - 2, +2d)}_{\text{EVOSV}} + b \underbrace{TCP_i(d, 0)}_{\text{TCSV}}$$

Tropical cyclone tracks from GRAPES-GEPS

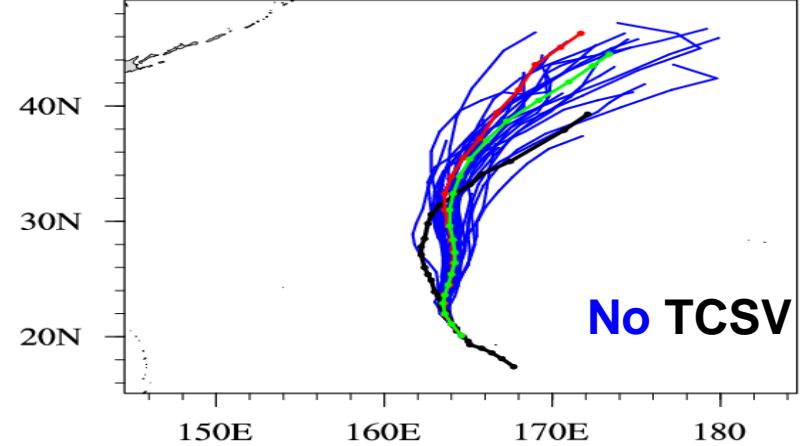
6 TC cases in 2017

RMSE/SPREAD of TC track



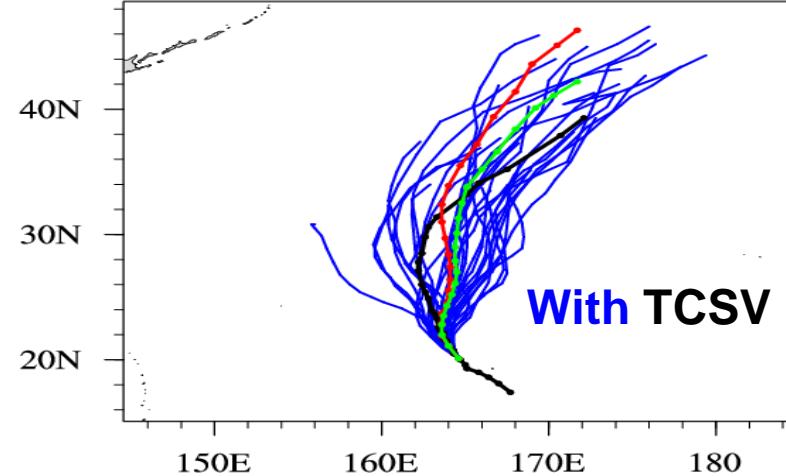
Ensemble Tracks of TC (1712) 120 h forecast based on 2017081212 UTC

tracks: OBS = black CTRL = red MEAN = green EPS members = blue



Ensemble Tracks of TC (1712) 120 h forecast based on 2017081212 UTC

tracks: OBS = black CTRL = red MEAN = green EPS members = blue



- SV-based initial perturbation
- **Representations of model uncertainties**
- The performance of GRAPES-GEPS
- Summary and future work

Stochastic Physics (1) -SPPT

Stochastically perturbed physics tendencies (**SPPT**) scheme

$$\delta X_p = \psi(\lambda, \phi, t) \delta X$$

Random perturbed
Physical tendency

Random
pattern

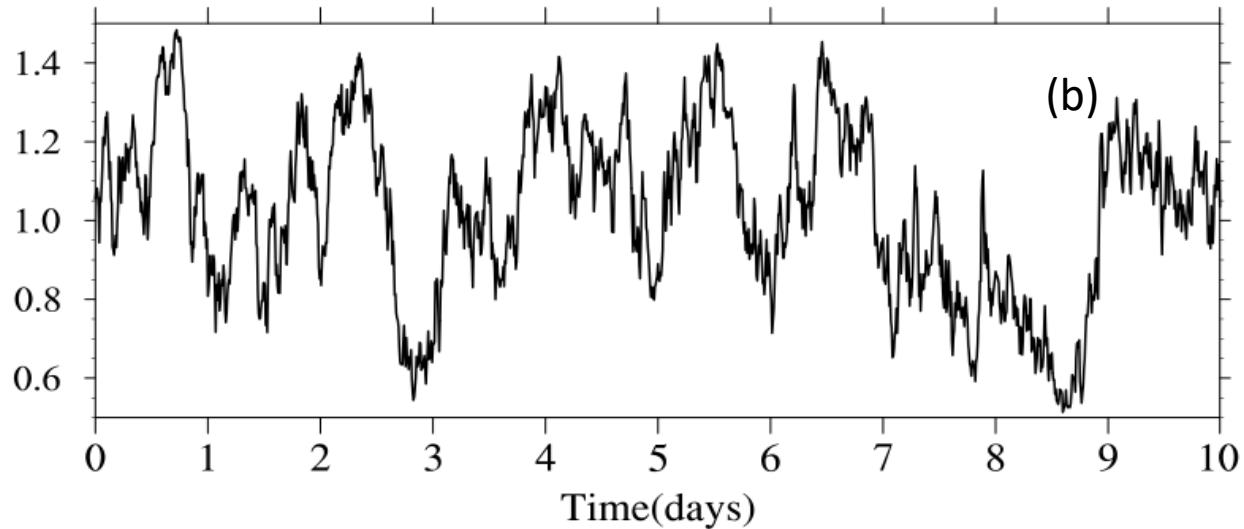
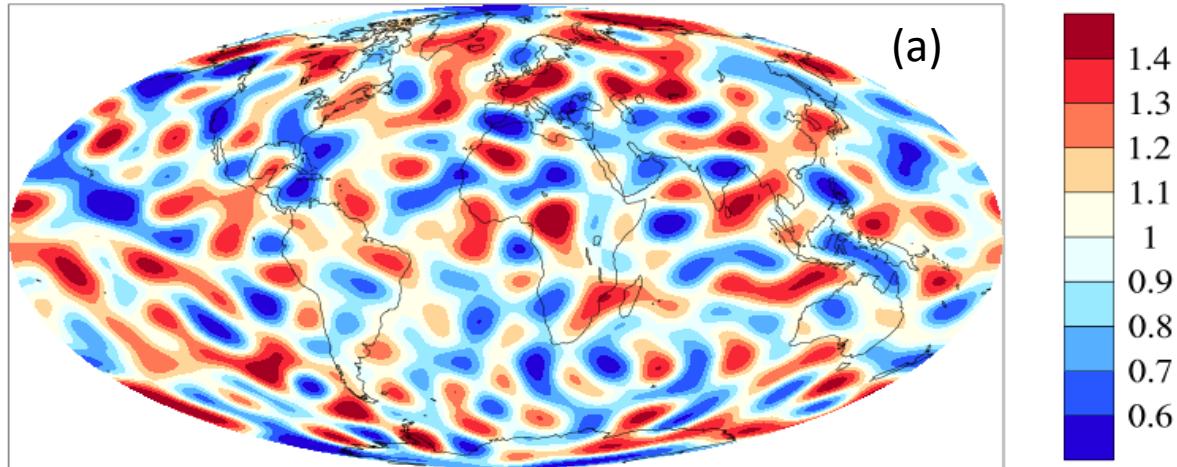
Physical
tendency

$$\psi(\lambda, \phi, t) = \mu + \sum_{l=1}^L \sum_{m=-l}^l \alpha_{l,m}(t) Y_{l,m}(\lambda, \phi)$$

$$\alpha_{l,m}(t + \Delta t) = e^{-\Delta t/\tau} \alpha_{l,m}(t) + \sqrt{\frac{4\pi\sigma^2(1-e^{-2\Delta t/\tau})}{L(L+2)}} R_{l,m}(t) \implies \text{First-order auto-regressive process}$$

- Random pattern
 - following **Gaussian distribution**
 - temporal decorrelation scales : **6h**
 - the lower and upper limit of random values: **[0.5,1.5]**
- Applying stochastic perturbation to model variables
(**u,v,T,q**)

Structure of random pattern used in SPPT



(a) the horizontal distribution;

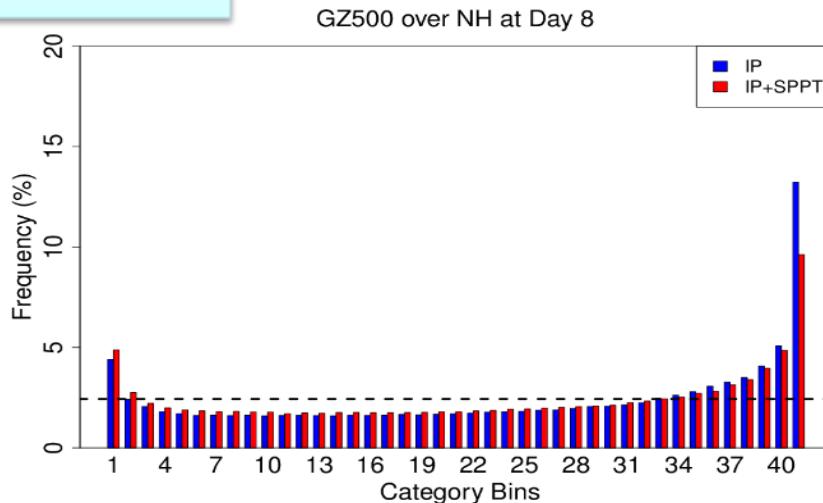
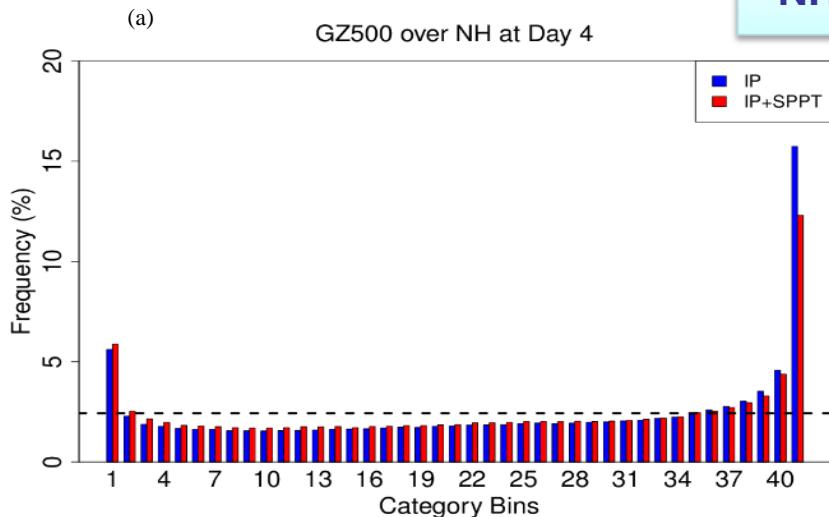
(b) time series of the random number value at an arbitrary model grid

The ensemble experiments with SPPT

exp1: INISVS
exp2: INISVS+SPPT

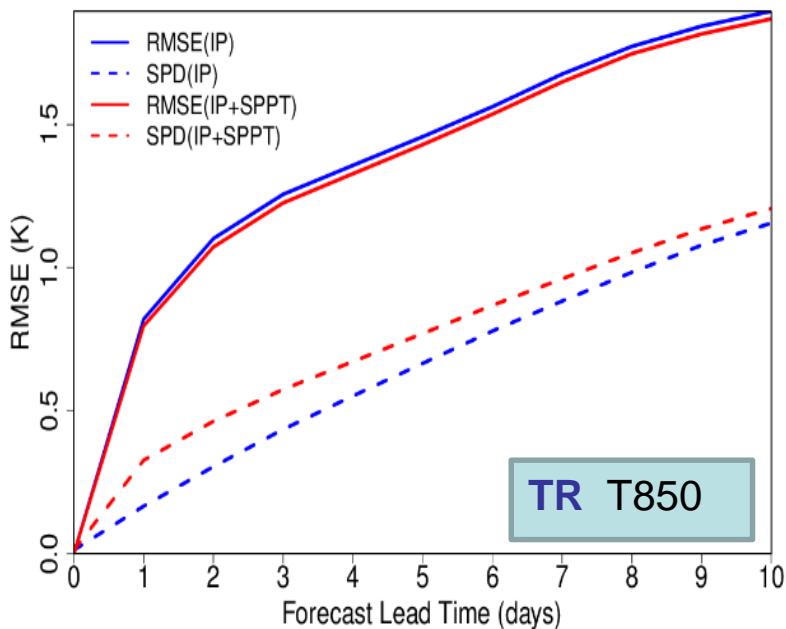
Talagrand Histogram

NH GZ500

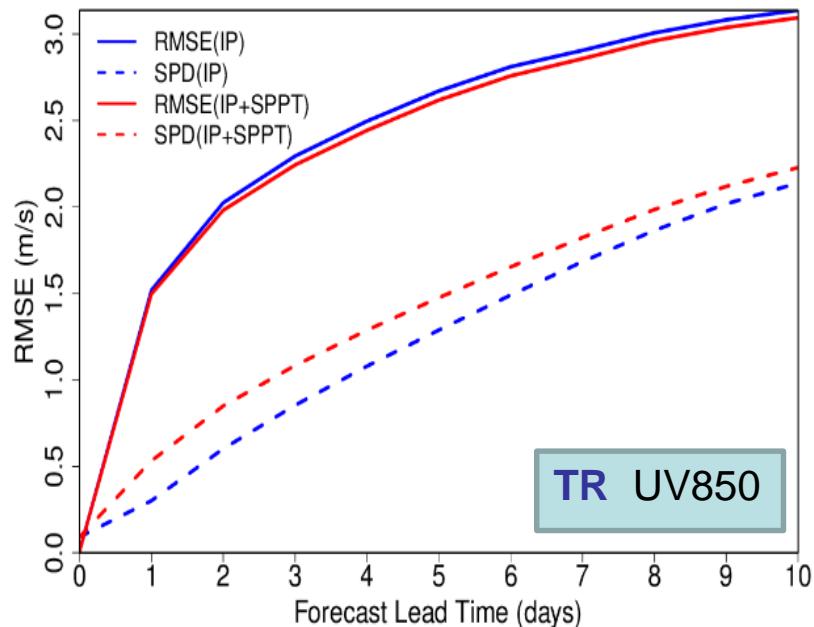


RMSE Spread skill

RMSE/SPD T850 over TR



RMSE/SPD UV850 over TR



Stochastic Physics (2) -SKEB

Stochastic kinetic energy backscatter (**SKEB**) scheme

- ✓ SKEB introduces horizontal wind (u,v) stochastically forcing terms though an added tendency terms:

(Charron et. al. 2010)

$$\left(\frac{\partial u}{\partial t} \right)_{\text{SKEB}} = S_u$$

$$S_u = -\frac{1}{a} \frac{\partial F_\psi}{\partial \phi}$$

$$\left(\frac{\partial v}{\partial t} \right)_{\text{SKEB}} = S_v$$

$$S_v = \frac{1}{a \cos \phi} \frac{\partial F_\psi}{\partial \lambda}$$

Stream-function forcing

$$F_\Psi = \frac{\alpha \Delta x}{\Delta t} \underbrace{\Psi(\lambda, \phi, t)}_{\text{3D random field}} \sqrt{\Delta t \underbrace{\hat{D}(\lambda, \phi, \eta, t)}_{\text{Dissipation rate}}}$$

3D random field

Dissipation rate

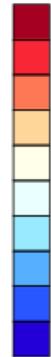
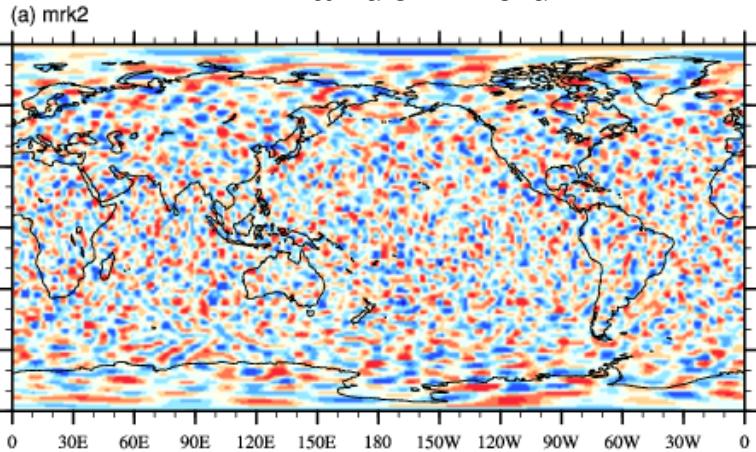
Random field (same random generator as SPPT with specified parameters)

from **explicit horizontal diffusion**

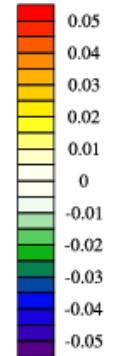
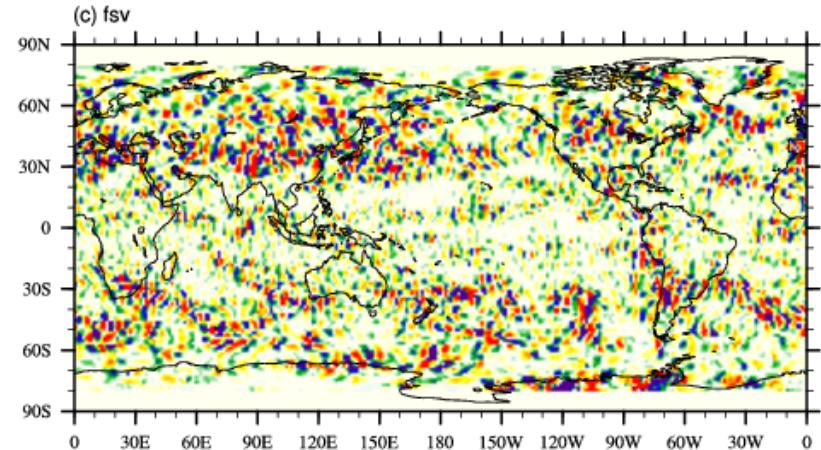
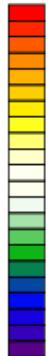
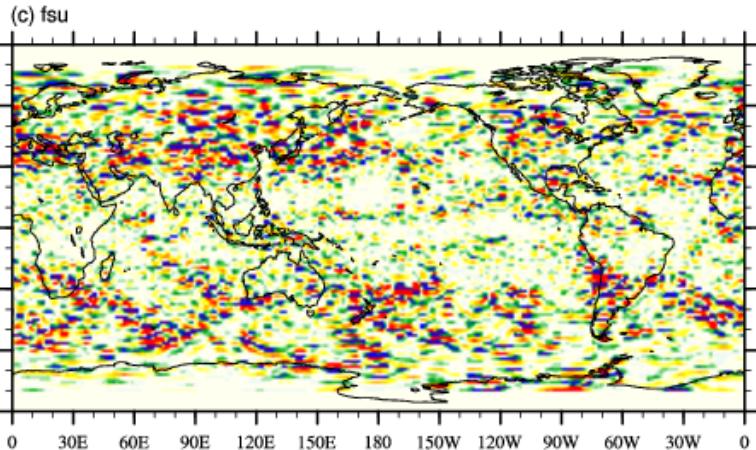
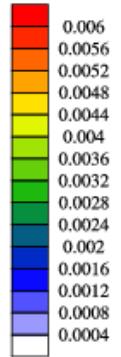
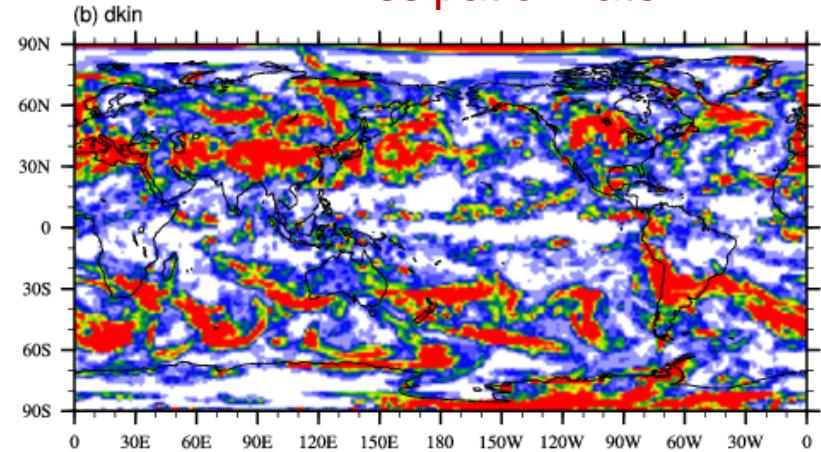
$$D_{\text{num}} = \sqrt{(u \times du)^2 + (v \times dv)^2}$$

Structure of u , v wind forcing of SKEB

Random field



Dissipation rate



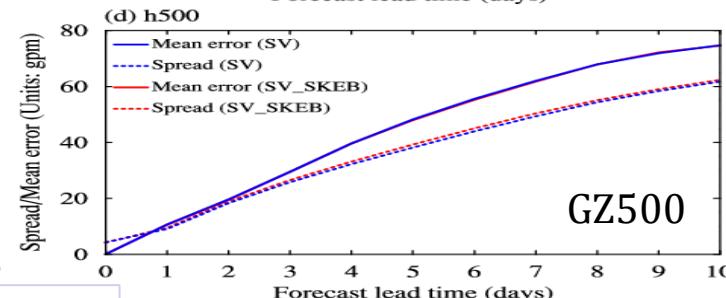
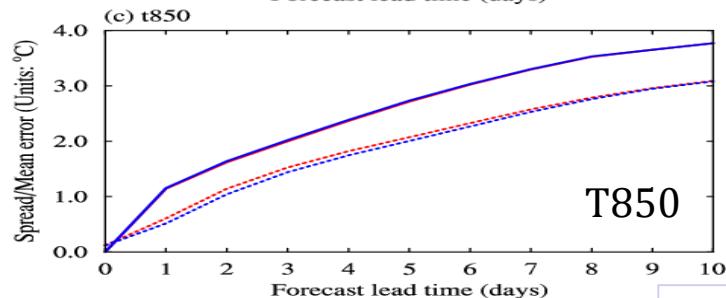
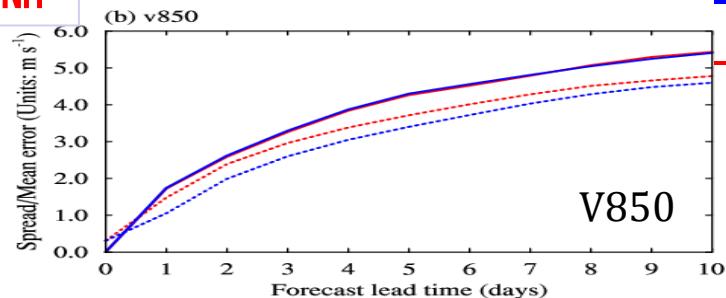
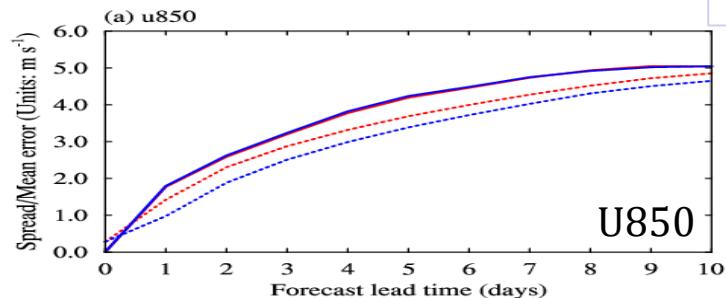
u wind forcing

v wind forcing

12 h forecast at model level 30 (initialized at 00 UTC 13 May, 2013)

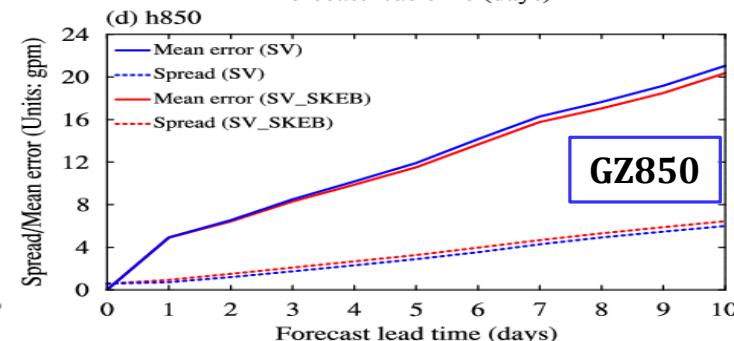
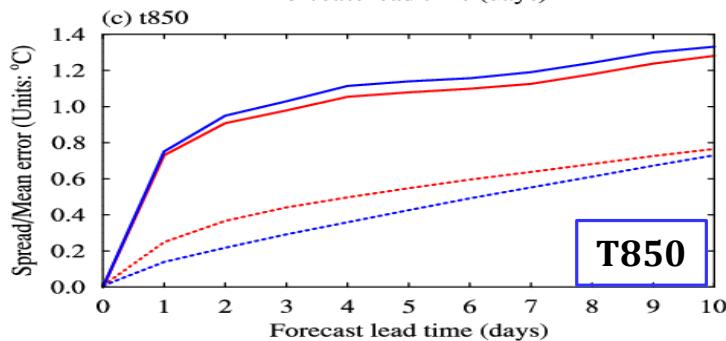
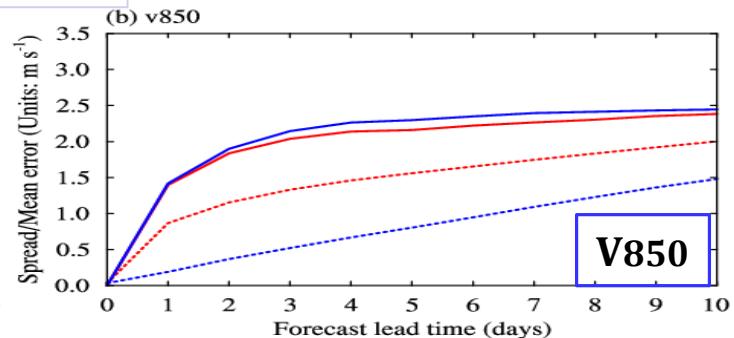
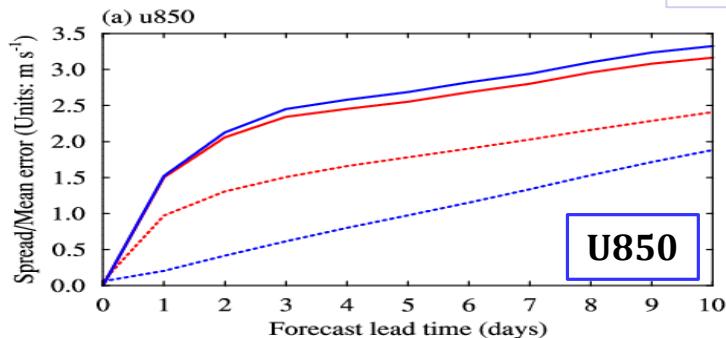
The GRAPES-GEPS with SKEB

NH



— SV
— SV+SKEB

Tropics



- SV-based initial perturbation
- The model uncertainties
- **The performance of GRAPES-GEPS**
- Summary and future work

Operational GRAPES-GEPS (since Dec. 2018)

- **GRAPES-GEPS** has been operationally running at CMA since 26 Dec 2018, replacing previous operational **T639-GEPS**

T639-GEPS

Forecast Model	T639L60
Resolution	0.28° ; 60 layer top at 0.1hPa
Initial Perturbation	Breeding Vector-based
Model perturbation	SPPT
Ensemble Size	15 (14 perturbed members+control)
Forecast length	15 days



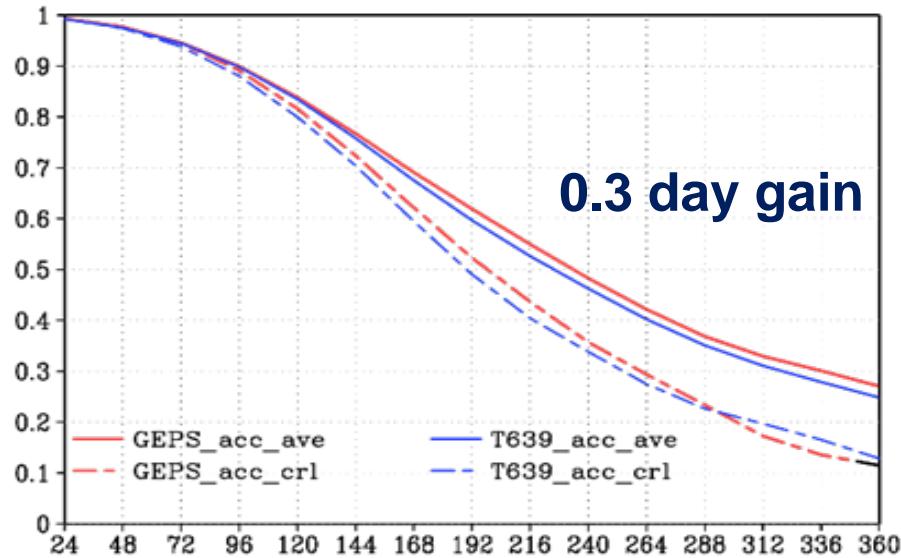
Operational GRAPES-GEPS

Forecast Model	GRAPES GFS
Resolution	0.5° × 0.5° ; 60 layer top at 3hPa
Initial Perturbation	SVs-based
Model perturbation	SPPT; SKEB
Ensemble Size	31 (30 perturbed members +control)
Forecast length	15 days

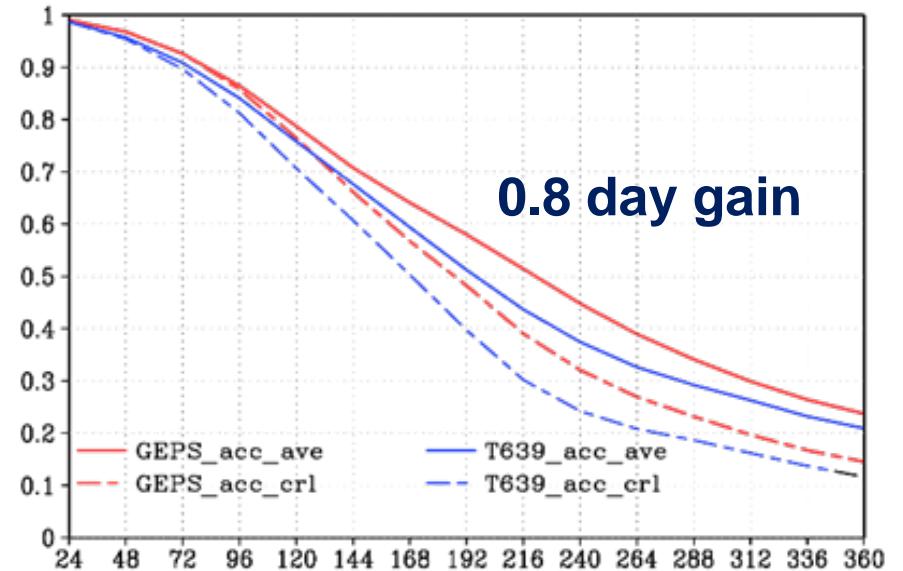
Performance of **GRAPES-GEPS** compared with **T639-GEPS** (1)



ACC, 500hpa位势高度场“北半球地区”
2016101512-2018043012

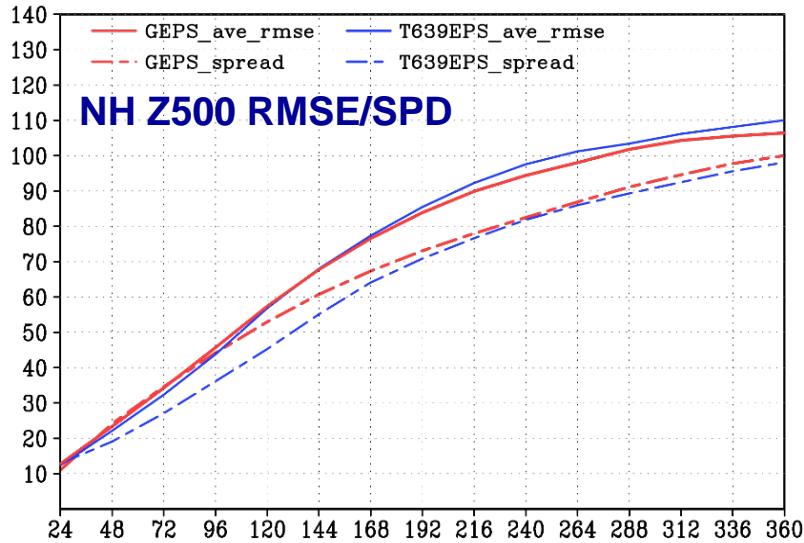


ACC, 500hpa位势高度场“南半球地区”
2016101512-2018043012

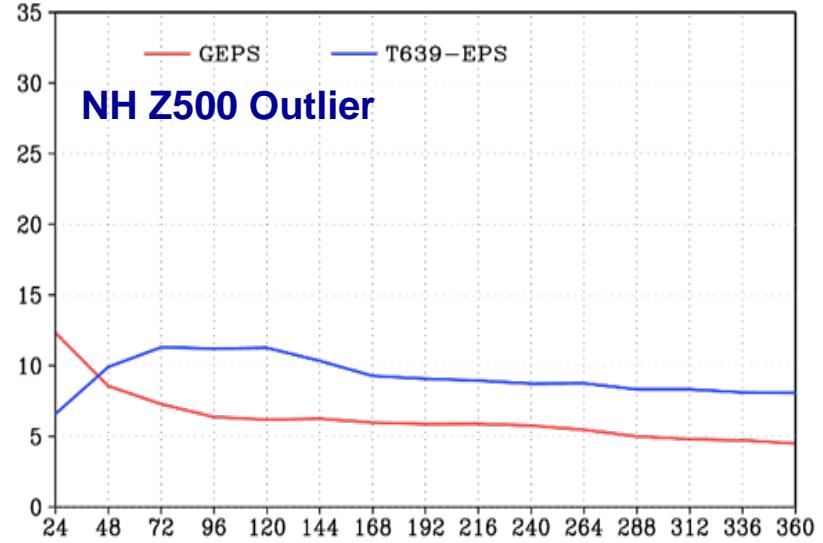


Performance of GRAPES-GEPS compared with T639-GEPS (2)

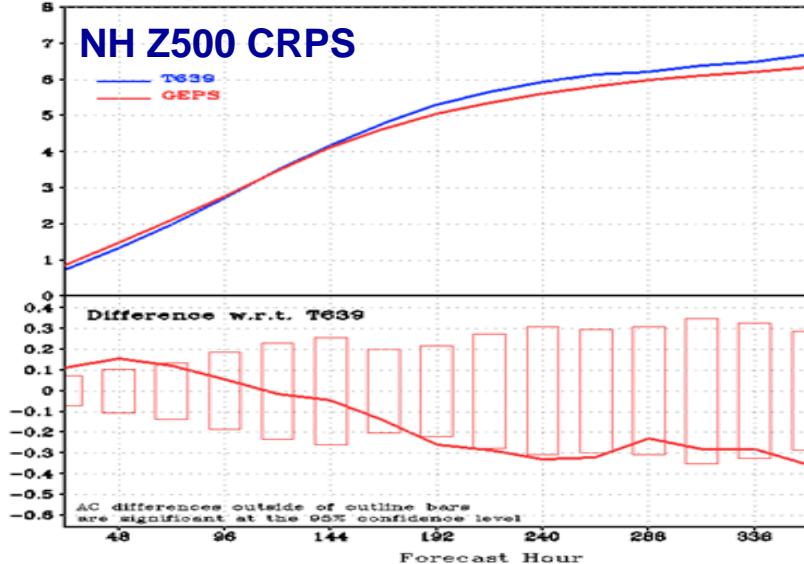
RMSE&Spread,500hpa位势高度场"北半球地区"
2017120112-2017123112



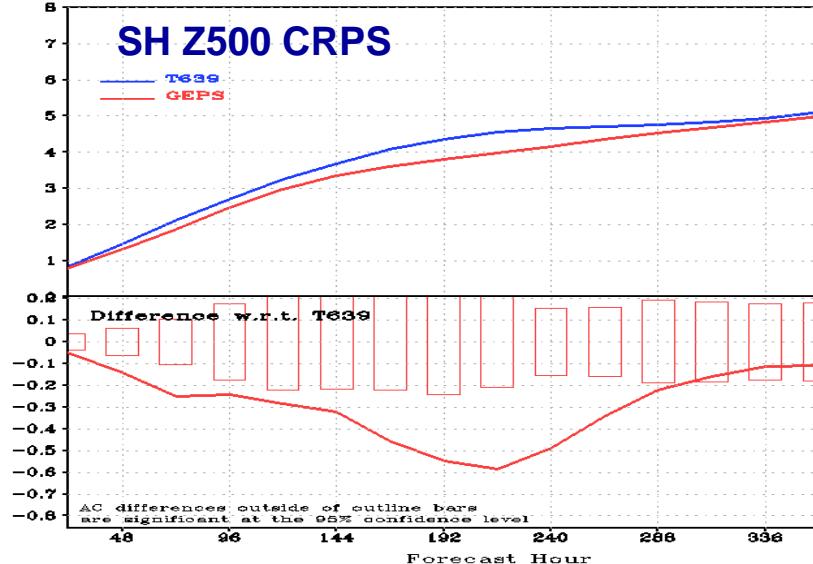
Outlier,500hpa位势高度场"北半球地区"
2017120112-2017123112



CRPS(dgm): HGT P500 Q2/NH 12Z, 20171201-20171231



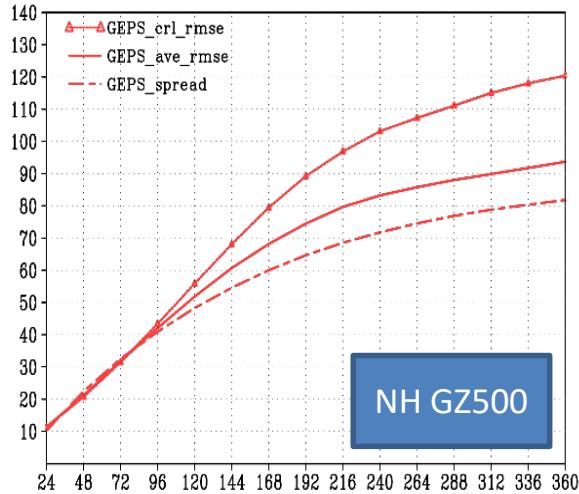
CRPS(dgm): HGT P500 Q2/SH 12Z, 20170801-20170831



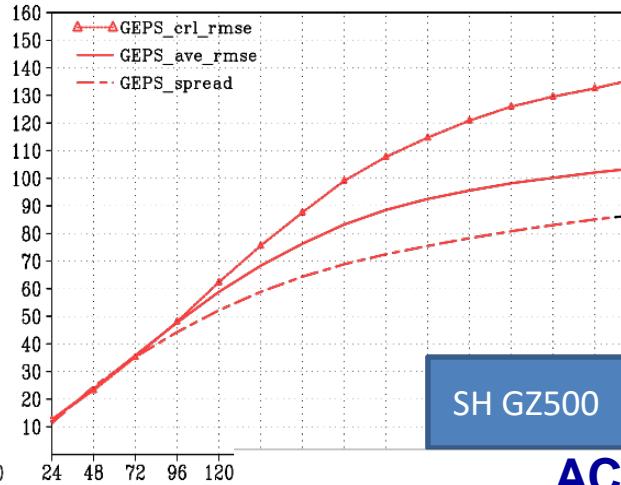
Performance of operational GRAPES-GEPS

RMSE/SPD (201901-201905)

RMSE&Spread,500hpa位势高度场"北半球地区"
2019010112-2019053112

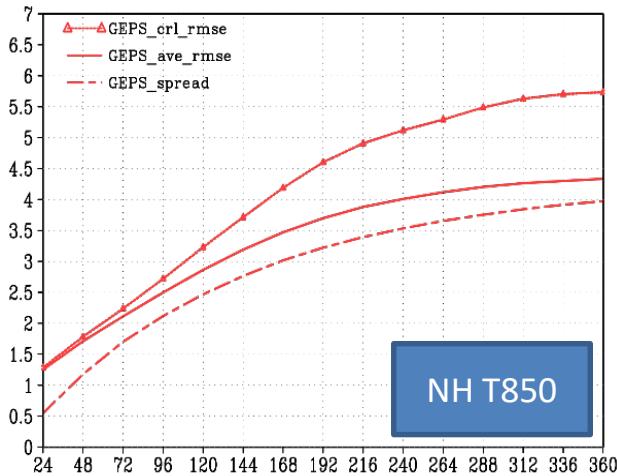


RMSE&Spread,500hpa位势高度场"南半球地区"
2019010112-2019053112

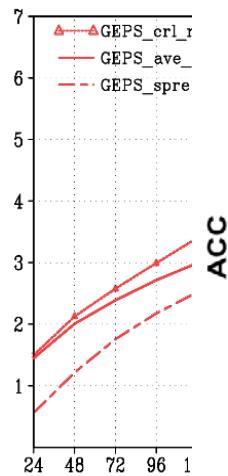


ACC of GZ500 at Day 7

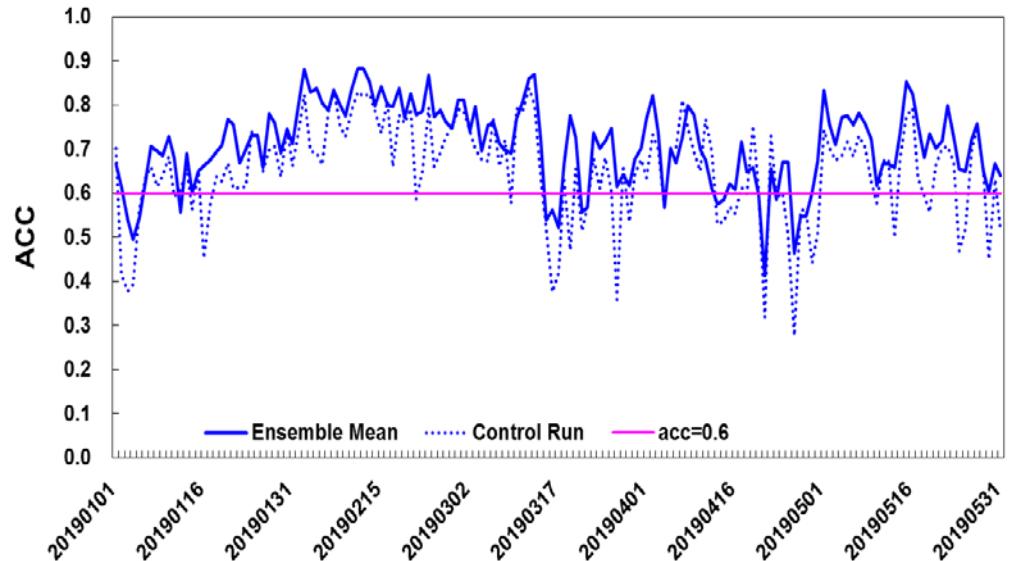
RMSE&Spread,850hpa温度场"北半球地区"
2019010112-2019053112



RMSE&Sp
20190101



GZ500 over NH grids of GRAPES_GEPS at 7 day



Forecast of blocking high at middle range

Example : 00 UTC 5 Feb.2019

The development Ural blocking high before breakout of cold wave

500hPa Spaghetti (5360、5680、5880)

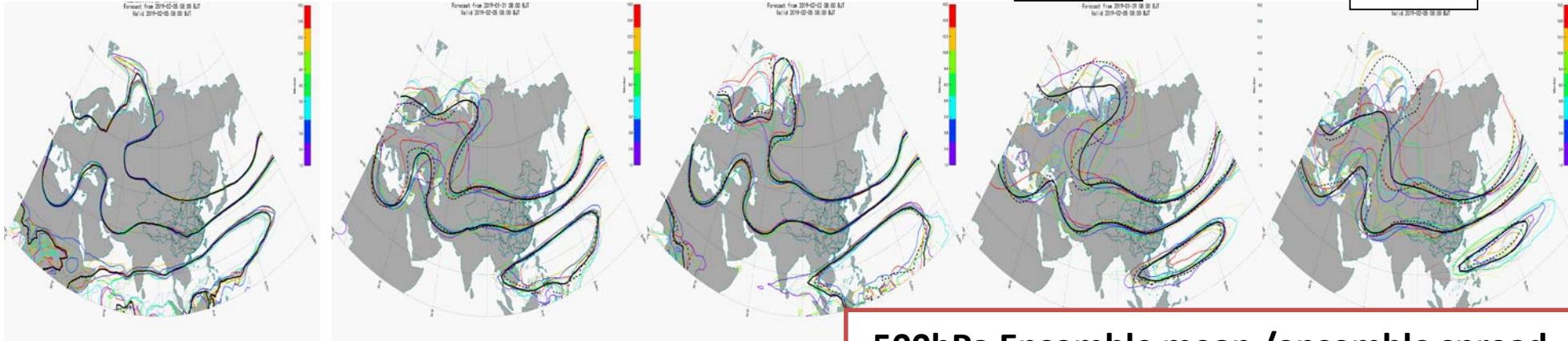
Analyses

T+3d

T+5d

T+7d

T+9d

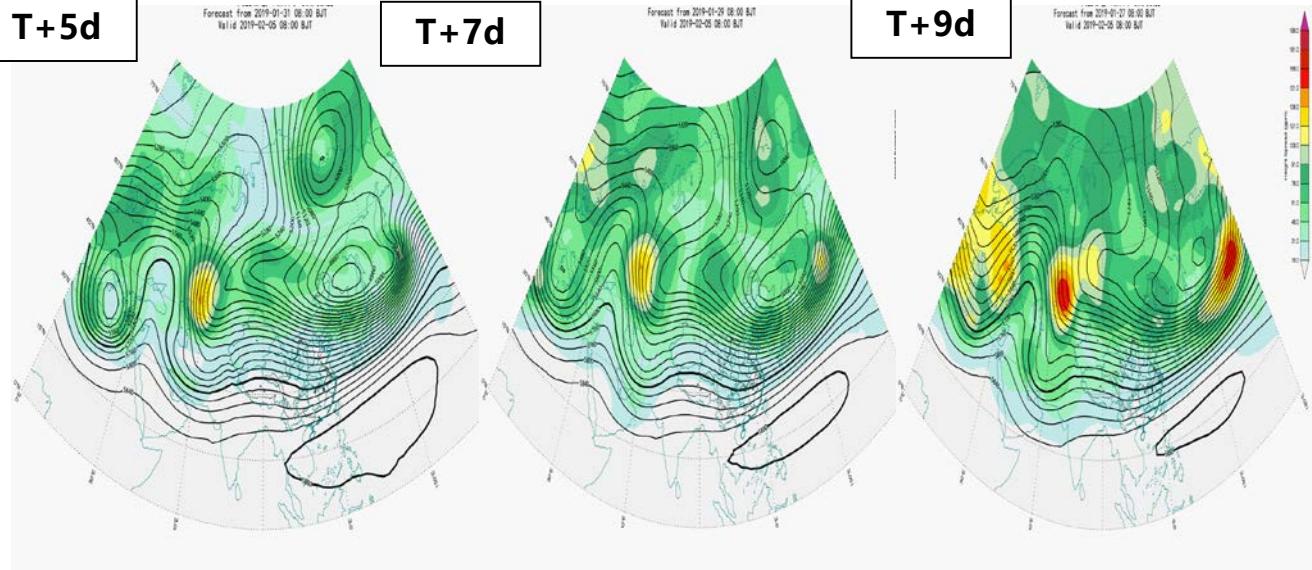


500hPa Ensemble mean /ensemble spread

T+5d

T+7d

T+9d

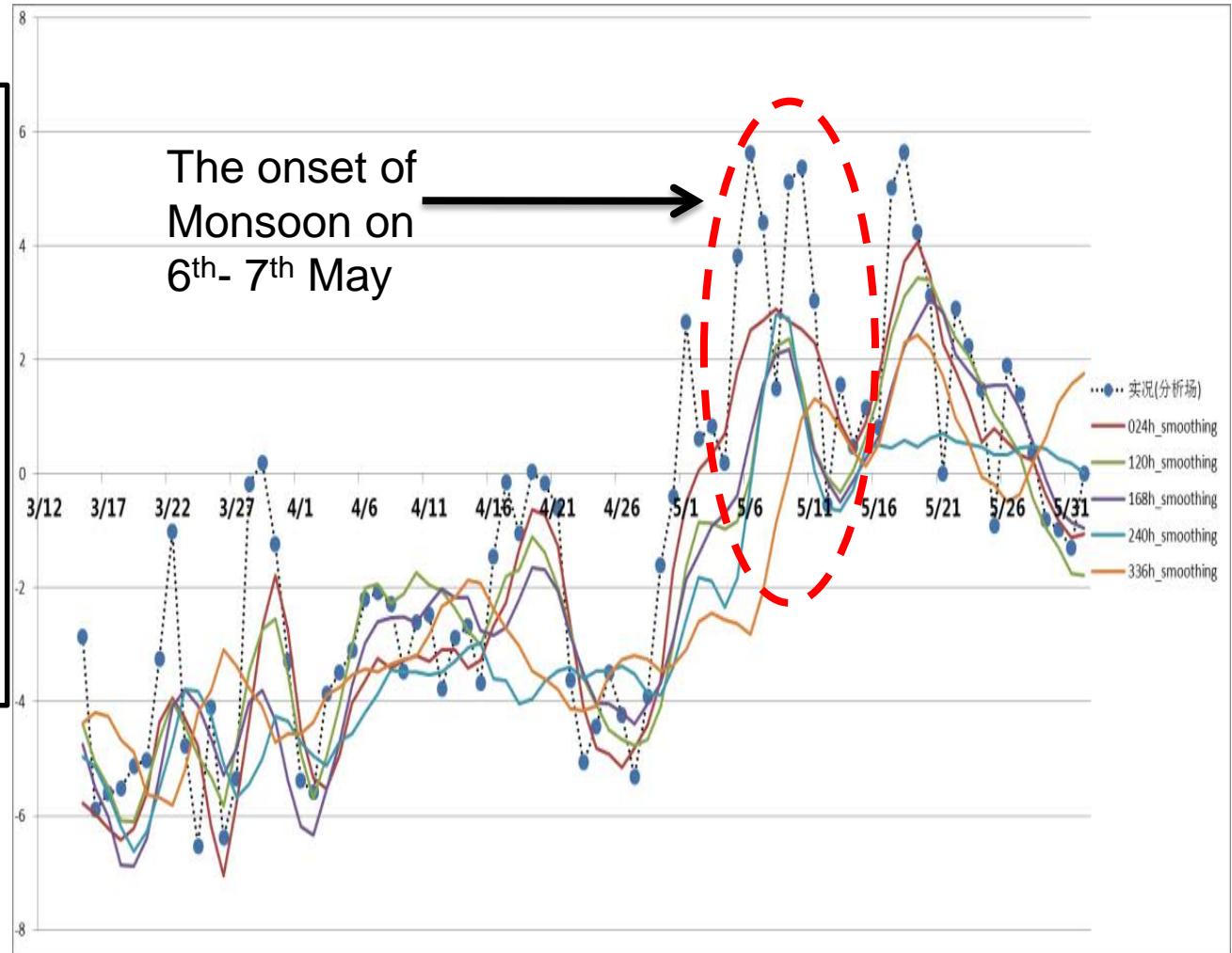


GRAPES_GEPS is able to give the useful information for the development of the Ural blocking high 7-10 days earlier

Forecast for onset of South China Sea Monsoon 2019

- The monsoon index

- Monitor Area of South China Sea monsoon 850hpa (10°-20°N, 110°-120°E)
- 850hpa Zonal wind and pseudo-equivalent potential temperature are used as index of onset of monsoon (by National Climate Center of CMA)



Dot line - Obs

Solid lines – forecasts at 1d,5d,7d,10d , and 14d

Summary and future work

- SV-based initial perturbation contribute the major performance of GRAPES-GEPS: ensemble spread and forecast skills
- The empirical parameters in the generation of SV-based initial perturbation will be tuned when GRAPES model is upgraded
- The improvement for TC SVs will be focused on the improvement of linearized moist physics
- The model uncertainty of GRAPES-GEPS will be focused on the improvement of existed SPPT and SKEB